MATLAB CODE FOR AN ENHANCED VIBRATING PARTICLES SYSTEM ALGORITHM

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ABSTRACT

Vibrating particles system (VPS) is a new meta-heuristic algorithm based on the free vibration of freedom system’s single degree with viscous damping. In this algorithm, each agent gradually approach to its equilibrium position; new agents are generated according to current agents and a historically best position. Enhanced vibrating particles system (EVPS) employs a new alternative procedure to enhance the performance of the VPS algorithm. Two different truss structures are investigated to demonstrate the performance of the VPS and EVPS weight optimization of structures.

Keywords: vibrating particles system algorithm; enhanced vibrating particles system algorithm; MATLAB code; truss structures.

Received: 8 September 2017; Accepted: 12 November 2017

1. INTRODUCTION

One of the most important applications of the optimization in knowledge engineering is optimal design. This design leads to correct use of what is limited in each engineering problems. Metaheuristic algorithms are usual tools to optimize problems in suitable time but these methods cannot ensure to gain the best answer. Structural optimization results in economical design and is an active topic in the field of civil and in particular structural engineering [1-5]. Meta-heuristic algorithms that are widely used in structural optimization are as follows:

Genetic Algorithms (GA) [6], Particle Swarm Optimization (PSO) [7], Charged System Search algorithm (CSS) [8], Ray Optimization (RO) [9], Colliding Bodies Optimization (CBO)[10], Cyclical parthenogenesis algorithm [11], Ant Colony Optimization (ACO) [12],

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Dolphin Echolocation algorithm (DEA) [13], Imperialist Competitive Algorithm (ICA) [14], Harmony Search (HS) algorithm [15], Grey wolf optimizer [16].

In this paper the vibrating particles system (VPS) algorithm [17] and the enhanced vibrating particles system (EVPS) [2] are briefly introduced and employed to weight optimization of some truss structures. The VPS algorithm is inspired by the free vibration of single degree of freedom systems with viscous damping. The EVPS algorithm employs some procedures to enhance the VPS algorithm performance. These procedures are employed to augment the ability of the standard VPS to perform a global search and prevent entrapment in local optima. The VPS and EVPS algorithms are used for weight optimization of two truss structures. Results imply that the performance of EVPS algorithm is enhanced in comparison to the standard VPS algorithm for these structures.

This paper is organized as follow: In the first section, introduction is presented. Vibrating particles system (VPS) and enhanced vibrating particles system (EVPS) algorithms are imposed in section 2. The formulation of the weight optimization of truss structures is performed in section 3. In the fourth section, two benchmark problems are investigated with VPS and EVPS algorithms. Conclusion is presented in last section. Computer code in MATLAB for EVPS algorithm is presented in Appendix 1, and a hypothetical objective function is presented in Appendix 2.

2. OPTIMIZATION ALGORITHMS

In this part, Vibrating Particles System (VPS) and Enhanced Vibrating Particles System (EVPS) algorithms are presented.

2.1 Vibrating particles system algorithm

Vibrating particles system (VPS) is a new meta-heuristic algorithm based on the free vibration of freedom system’s single degree with viscous damping [18]. In this meta-heuristic algorithm, firstly the initial agents are generated in permissible range by:

\[ x_i^j = x_{min} + rand \cdot (x_{max} - x_{min}) \]  

where \( x_i^j \) is the \( j \)th variable of the \( i \)th particle. \( x_{min} \) and \( x_{max} \) are the starting and ending points of permissible search space for the \( j \)th variable and \( rand \) is a random number in the range of \([0, 1]\).

In the VPS algorithm three parameters are defined as:
1. \( HB \) (the historically best position of the entire population) is the best candidate until that iteration.
2. \( GB \) (a good particle) is selected randomly between partially best answers in each iteration.
3. \( BP \) (a bad particle) is selected randomly between partially worst answers in each iteration.

A descending function according to Eq. (2) is defined. This parameter is presented to include the effect of the damping level in the vibration.
where \( \text{iter} \) is the number of current iteration, \( \text{iter}^{\text{max}} \) is the total number of iterations and \( \alpha \) is a constant value. Creating the next agents in VPS algorithm is updated using the following equation:

\[
x_i^j = \omega_1 \left[ D.A. \text{rand1} + \text{HB}^l \right] + \omega_2 \left[ D.A. \text{rand2} + \text{GP}^l \right] + \omega_3 \left[ D.A. \text{rand3} + \text{BP}^l \right]
\]

\[
A = \left[ \omega_1 \left( \text{HB}^l - x_i^l \right) \right] + \left[ \omega_2 \left( \text{GP}^l - x_i^l \right) \right] + \left[ \omega_3 \left( \text{BP}^l - x_i^l \right) \right]
\]

\[
\frac{\omega_1 + \omega_2 + \omega_3 = 1}{\text{iter}^{\text{max}}} = \frac{\text{iter}}{\text{iter}^{\text{max}}}
\]

where \( \omega_{1,2} \) and \( \omega_3 \) are of relative importance to \( \text{HB} \), \( \text{GB} \) and \( \text{BP} \), respectively and ran1, ran2 and ran3 are random numbers uniformly distributed in the range \([0, 1]\).

A parameter like \( p \) (within 0 to 1) is defined to accelerate the convergence of the VPS algorithm. This parameter is compared with \( \text{rand} \) and if \( p < \text{rand} \), then \( \omega_1 = 0 \) and \( \omega_2 = 1 - \omega_1 \).

Pseudo code of the vibrating particles system algorithm is presented in Fig. 1 adopted from Kaveh and Ilchi Ghazaan [19].

```
procedure Vibrating Particles System (VPS)
Initialize algorithm parameters
Initial positions are created randomly
The values of objective function are evaluated and HB is stored
While maximum iterations is not fulfilled
  for each particle
    The GP and BP are chosen
    if P<rand
      \( w_1=0 \) and \( w_2=1-w_1 \)
    end if
    for each component
      New location is obtained by Eq. (3)
    end for
    Violated components are regenerated by harmony search-based handling approach
  end for
  The values of objective function are evaluated and HB is updated
end while
end procedure
```

Figure 1. Pseudo code of the standard vibrating particles system algorithm [19]

When an agent violates a boundary, it is changed by the harmony search-based side constraint handling approach. In this technique, \( \text{HMCR} \) (harmony memory considering rate) parameter determines whether the violating component should be changed with the corresponding value in \( \text{HB} \) or it must be selected from the permissible search space. Also, if changed with \( \text{HB} \), there is a parameter, \( \text{PAR} \) (pitch adjusting rate), that determines whether this value should be changed with the neighboring value or not. This process is repeated for \( \text{iter}^{\text{max}} \) times.

2.2. Enhanced vibrating particles system algorithm

In this section, Enhanced Vibrating Particles System (EVPS) is presented which in main follows [2]. This improvement results in increasing the convergence speed, augmenting the
ability of search, helping the EVPS to escape from local optima and overall resulting in better results. Changes to the standard version of the VPS algorithm are as follows:

In this method, Memory parameter acts as HB with the difference that it saves Memorysize number of the best historically positions from the entire population. It should be noted that if the best answer of each iteration is better than the worst value of the Memory, it should replace the worst value in the memory.

OHb (one of the best historically positions in entire population) is one row of Memory that is selected randomly. HB is replaced with Memory in the EVPS algorithm. Another change made to the VPS algorithm is that Eq. (4) is replaced with Eq. (3). In Eq. (4), one of the (a), (b) and (c) equations are used with the possibility of \( \omega_{1,2} \) and \( \omega_{3} \), respectively.

\[
x_{i}^{j} = \begin{cases} 
D.A.rand1 + OHb^{j} & (a) \\
D.A.rand2 + GP^{j} & (b) \\
D.A.rand3 + BP^{j} & (c) \\
(\pm1)(OHb^{j} - x_{i}^{j}) & (a) \\
(\pm1)(GP^{j} - x_{i}^{j}) & (b) \\
(\pm1)(BP^{j} - x_{i}^{j}) & (c) 
\end{cases}
\]

where (±1) are used randomly. It should be noted that OHb, GP and BP are determined for every agent independently. Other parts of the EVPS are exactly the same as in the standard VPS algorithm.

3. FORMULATION

In this formulation, the aim is to minimize the weight of structures besides satisfying certain design constraints. These constraints include strength and displacements constraints according to LRFD-AISC specification [20]. The mathematical formulation can be expressed as:

Find \( \{x\} = [x_{1}, x_{2}, \ldots, x_{ng}] \quad x_{i} \in S_{j} \)

To minimize \( W(\{x\}) = \sum_{i=1}^{nm} \rho_{i} A_{i} L_{i} \) \hspace{1cm} (5)

Subjected to

\[
\begin{align*}
& g_{j}(\{x\}) \leq 0, \quad j = 1, 2, \ldots, nc \\
& x_{i\min} \leq x_{i} \leq x_{i\max}
\end{align*}
\]

where \( \{x\} \) is a set of design variables containing the cross sectional area; \( ng \) is the numbers of member groups (number of design variables); \( W(\{x\}) \) is the weight of the structure; \( nm \) is the number of elements of the structure; \( nc \) is the number of constraints; \( \rho_{i} \) presents the
material density of \(i\)th member; \(A_i\) and \(L_i\) denote the cross-sectional area and the length of member \(i\), respectively.

4. NUMERICAL PROBLEMS

Two benchmark problems are presented to investigate the performance of the VPS and EVPS algorithms. The values of population size, the total number of iteration, \(p\), \(w_1\), \(w_2\), \(HMCR\), \(PAR\) and \(Memorysize\) are 50, 1000, 0.2, 0.3, 0.3, 0.95, 0.1 and 4 for all problems, respectively. Thirty independent optimization runs are carried out for all the problems.

4.1 A 72-bar spatial truss

For the 72-bar spatial truss structure shown in Fig. 2, the elements are categorized in 16 design groups:

(1) \(A1\_A4\), (2) \(A5\_A12\), (3) \(A13\_A16\), (4) \(A17\_A18\), (5) \(A19\_A22\), (6) \(A23\_A30\), (7) \(A31\_A34\), (8) \(A35\_A36\), (9) \(A37\_A40\), (10) \(A41\_A48\), (11) \(A49\_A52\), (12) \(A53\_A54\), (13) \(A55\_A58\), (14) \(A59\_A66\) (15), \(A67\_A70\), and (16) \(A71\_A72\).

The material density is \(0.1\ lb/\text{in}^3\) and the modulus of elasticity is taken as \(10,000\ ksi\). The members are subjected to the stress limits of \(\pm 25\ ksi\). The nodes are subjected to the displacement limits of \(\pm 0.25\ in\). The minimum permitted cross-sectional area of each member is taken as \(0.10\ in^2\), and the maximum cross-sectional area of each member is \(4.00\ in^2\). The loading conditions are considered as:

1. Loads 5, 5 and -5 kips in the \(x\), \(y\) and \(z\) directions at node 17, respectively.
2. A load -5 kips in the \(z\) direction at nodes 17, 18, 19 and 20.

Table 1 shows the results obtained by VPS and EVPS algorithms. Fig. 3 presents the convergence diagrams for VPS and EVPS algorithms. According to Table 1, the lightest weight is achieved by EVPS and this algorithm has reached best average weight among the other algorithms. Fig. 3 shows the best of one hundred iterations convergence history for the VPS and EVPS algorithms for the best answer.
Figure 2. Schematic of the 72-bar spatial truss

Table 1: Comparison of the VPS and EVPS results with other algorithms for the 72-bar spatial truss

<table>
<thead>
<tr>
<th></th>
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<th></th>
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<td>0.39</td>
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<td>4 A17-A18</td>
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<td>0.592</td>
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<td>0.1004</td>
<td>0.100002</td>
<td>0.100002</td>
<td>0.100002</td>
<td>0.1003</td>
<td>0.105423</td>
<td>0.107943</td>
</tr>
<tr>
<td>8 A35-A36</td>
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<td>0.107</td>
<td>0.1001</td>
<td>0.100004</td>
<td>0.1</td>
<td>0.100005</td>
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<td>0.100734</td>
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<tr>
<td>9 A37-A40</td>
<td>1.2476</td>
<td>1.303</td>
<td>1.2522</td>
<td>1.266652</td>
<td>1.202484</td>
<td>1.286803</td>
<td>1.2592</td>
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<td>1.26445</td>
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<td>10 A41-A48</td>
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<td>0.511</td>
<td>0.5033</td>
<td>0.511534</td>
<td>0.505656</td>
<td>0.508058</td>
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<td>0.100002</td>
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<td>0.1</td>
<td>0.1001</td>
<td>0.100002</td>
<td>0.1</td>
<td>0.100002</td>
<td>0.1003</td>
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<td>13 A55-A58</td>
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<td>1.8365</td>
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<td>1.86922</td>
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<td>0.508</td>
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<td>0.101</td>
<td>0.1</td>
<td>0.1</td>
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<td>0.100038</td>
<td>0.1</td>
<td>0.107713</td>
<td>0.1</td>
</tr>
<tr>
<td>16 A71-A72</td>
<td>0.1</td>
<td>0.102</td>
<td>0.1004</td>
<td>0.100001</td>
<td>0.100001</td>
<td>0.100015</td>
<td>0.1</td>
<td>0.10143</td>
<td>0.100001</td>
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<tr>
<td>Best weight (lb)</td>
<td>379.85</td>
<td>380.24</td>
<td>380.458</td>
<td>379.61</td>
<td>379.93</td>
<td>379.65</td>
<td>379.93</td>
<td>384.1197</td>
<td>379.6482</td>
</tr>
<tr>
<td>Worst weight (lb)</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>379.74</td>
<td>380.53</td>
<td>379.76</td>
<td>380.2073</td>
<td>392.9363</td>
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<tr>
<td>Average weight (lb)</td>
<td>382.08</td>
<td>383.16</td>
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<td>379.66</td>
<td>380.20</td>
<td>380.30</td>
<td>380.5306</td>
<td>387.7259</td>
<td>379.7143</td>
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</table>

*CBO and ECBO algorithms were used for optimization of this problem by Kaveh and Mahdavi [23] and Kaveh and Ilchi Ghazaan [24], respectively. These results obtained by the authors in this article.
4.1 A 582-bar tower truss

The schematic of the 582-bar tower truss with the height of 80 m is presented in Fig. 4. The symmetry of the tower around x-axis and y-axis is considered to group the 582 members into 32 independent size variables. A single load case is considered such that it consists of lateral loads of 5.0 kN applied in both x and y directions and a vertical load of -30 kN applied in the z-direction at all nodes of the tower. A discrete set of 137 economical standard steel sections selected from W-shape profile list based on area and radii of gyration properties is used to size the variables. The lower and upper bounds on size variables are taken as 39.74 cm$^2$ and 1387.09 cm$^2$, respectively. The stress limitations of the members are imposed according to the provisions of ASD-AISC [20]. The other constraint is the limitation of nodal displacements (these should not be more than 8.0 cm or 3.15 in. in any direction). Also, the maximum slenderness ratio is limited to 300 for tension members, and it is recommended to be 200 for compression members according to ASD-AISC design code provisions [20]. Table 2 shows the results obtained by VPS and EVPS algorithms. According to Table 2, the EVPS algorithm has reached better answer in comparison to the standard VPS algorithm in the best, worst and average answers. Fig. 5 presents the allowable and existing stress ratio and displacement values in 3 directions for the VPS and EVPS algorithms. Fig. 6 shows the best of one hundred iterations convergence histories for the VPS and EVPS algorithms for the best answer.
Figure 4. Schematic of the 582-bar tower truss

Table 2: Comparison of the VPS and EVPS results with other algorithms for the 582-bar tower truss

<table>
<thead>
<tr>
<th>Element Group</th>
<th>PSO*</th>
<th>CBO</th>
<th>ECBO</th>
<th>DHPASCO [27]</th>
<th>SDE [1]</th>
<th>VPS</th>
<th>EVPS</th>
</tr>
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<tr>
<td>1</td>
<td>39.74186</td>
<td>39.74186</td>
<td>39.74186</td>
<td>45.68</td>
<td>39.74186</td>
<td>41.87088</td>
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<td>2</td>
<td>136.1288</td>
<td>136.1288</td>
<td>163.2255</td>
<td>136.13</td>
<td>136.1288</td>
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<td>136.1288</td>
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<tr>
<td>3</td>
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<td>4</td>
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<td>45.67733</td>
<td>45.67733</td>
<td>45.68</td>
<td>45.67733</td>
<td>45.67733</td>
<td>45.67733</td>
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<tr>
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<td>85.80628</td>
<td>81.29016</td>
<td>94.19336</td>
<td>92.9</td>
<td>92.90304</td>
<td>74.1934</td>
<td>90.96756</td>
</tr>
</tbody>
</table>
Worst weight (m$^3$)  21.89  21.69  21.71  N/A  N/A  24.1290  22.0811
Average weight (m$^3$)  21.57  21.52  21.37  N/A  N/A  23.2414  21.5548

*This truss was optimized using the PSO algorithm by Kaveh and Talatahari [26] but the reported results in this article are obtained by authors.
In this paper a code is developed for an enhanced version of the vibrating particles system (EVPS). Two well-studied weight optimization of steel truss structures problems are investigated to show the efficiently of the EVPS in comparison with its standard version VPS. In the paper, EVPS and VPS algorithms are used for continuous and discrete optimization problems. For the considered examples, the EVPS algorithm has reached better results compared to the VPS algorithm and speed of convergence is higher. The results of two benchmark problems illustrate that the EVPS has a good performance and it can be utilized for other optimization problems. The results show that the EVPS is also competitive with other meta-heuristic algorithms. Finally, MATLAB code for the EVPS algorithm is presented in Appendix 1 and a hypothetical objective function is presented in Appendix 2.
REFERENCES


**APPENDIX 1: EVPS CODE IN MATLAB (THIS CODE IS APPLIED IN VPS CODE [19])**

```matlab
The EVPS code in MATLAB
% Enhanced VIBRATING PARTICLES SYSTEM - EVPS
% clear memory
clear all
% Initializing variables
popSize=50; % Size of the population
nVar=4; % Number of optimization variables
maxIt=1000; % Maximum number of iteration
xMin=-100; % Lower bound of the variables
xMax=100; % Upper bound of the variables
alpha=0.05;
w1=0.3;
w2=0.3;
w3=1-w1-w2;
p=0.2; % With the probability of (1-p) the effect of BP is ignored in updating
PAR=0.1;
HMCR=0.95;
Memorysize=4;
result=zeros(popSize,nVar+1);
Memory=zeros(Memorysize,nVar+1);
neighbor=0.1; % Parameters for handling the side constraints
% Initializing particles
position=(xMin+rand(popSize,nVar).*(xMax-xMin));
```
% Search
agentCost=zeros(popSize,3); % Array of agent costs
HBV=zeros(popSize,nVar+2); % Historically best matrix
for iter=1:maxIt % Evaluating and storing
    for m=1:popSize
        [penalizedWeight, weight]=SphereFun(position(m,:)); % Evaluating the objective function for each particle
        agentCost(m,1)=penalizedWeight;
        agentCost(m,2)=m;
        agentCost(m,3)=weight;
    end
    sortedAgentCost=sortrows(agentCost);
    for m=1:popSize
        if iter==1 || agentCost(m,1)<HBV(m,1)
            HBV(m,1)=agentCost(m,1);
            HBV(m,2)=agentCost(m,3);
            for n=1:nVar
                HBV(m,n+2)=position(m,n);
            end
        end
    end
    sortedHBV=sortrows(HBV);
    result(iter,1)=sortedHBV(1,1);
    result(iter,2:nVar+1)=sortedHBV(1,3:nVar+2);
    if iter==1
        for i=1:Memorysize
            Memory(i,1)=sortedHBV(i,1);
            Memory(i,2:nVar+1)=sortedHBV(i,3:nVar+2);
        end
    end
    if Memory(Memorysize,1)>sortedHBV(1,1)
        Memory(Memorysize,1)=sortedHBV(1,1);
        Memory(Memorysize,2:nVar+1)=sortedHBV(1,3:nVar+2);
    end
    Memory=sortrows(Memory);
% Updating particle positions
D=(iter/maxIt)^(-alpha);
for m=1:popSize
    templ=ceil(unifrnd(1,popSize/2,1));
    temp2=ceil(unifrnd(popSize/2,popSize,1));
    temp11=round(unifrnd(1,Memorysize,1));
    if p<rand
        w3=0;
        w2=1-w1;
    end
for n=1:nVar
    if rand<w3
        \( A(m,n) = (-1)^{\lceil \text{randn()} \rceil} \cdot (\text{position}(\text{sortedAgentCost}(\text{temp2}, 2), n) - \text{position}(m, n)) \)
        \( \text{position}(m, n) = D \cdot A(m, n) \cdot \text{rand} + \text{position}(\text{sortedAgentCost}(\text{temp2}, 2), n) \)
    elseif rand<w2
        \( A(m,n) = (-1)^{\lceil \text{randn()} \rceil} \cdot (\text{position}(\text{sortedAgentCost}(\text{temp1}, 2), n) - \text{position}(m, n)) \)
        \( \text{position}(m, n) = D \cdot A(m, n) \cdot \text{rand} + \text{position}(\text{sortedAgentCost}(\text{temp1}, 2), n) \)
    else
        \( A(m,n) = (-1)^{\lceil \text{randn()} \rceil} \cdot (\text{Memory}(\text{temp11}, 1+n) - \text{position}(m, n)) \)
        \( \text{position}(m, n) = D \cdot A(m, n) \cdot \text{rand} + \text{Memory}(\text{temp11}, 1+n) \)
    end
end
w2=0.3;w3=1-w1-w2;
end

% Handling the side constraints
for m=1:popSize
    for n=1:nVar
        if position(m,n)<xMin || position(m,n)>xMax
            temp1=rand; temp2=rand; temp3=ceil(rand*popSize);
            if temp1<=HMCR & temp2<=(1-PAR)
                position(m,n)=sortedHBV(temp3, 2+n);
            elseif temp1<=HMCR & temp2>(1-PAR)
                position(m,n)=sortedHBV(temp3, 2+n)+neighbor;
                if position(m,n)>xMax
                    position(m,n)=sortedHBV(temp3, 2+n)-2*neighbor;
                end
            else
                position(m,n)=xMin+(rand*(xMax-xMin));
            end
        end
    end
end

iter
sortedHBV(1,1)
end
% Saving the results
xlswrite('result.xls',result);
APPENDIX 2: A HYPOTHETICAL OBJECTIVE FUNCTION

Function [penalizedWeight, weight] = SphereFun(x)
%% If there is any violation:
% Penalty = sum of violations
% CP = Coefficient of penalty
% penalizedWeight = sum(x.^2)*(1+CP*Penalty);
penalizedWeight = sum(x.^2);
weight = sum(x.^2);
end